

### The Merits of a $K^\pm$ Tag for the BCD

In the EOI we discussed a lepton tag and hinted at other possibilities. Here we examine the possibility of tagging on the sign of a charged Kaon from the decay of the second  $B$  in the event. Such a Kaon would not reconstruct to the primary event vertex. This tag might be combined with a secondary-vertex trigger if the latter can be devised. It certainly could be used with a dilepton trigger, which would be useful in enlarging our samples of tagged  $B \rightarrow J/\psi X$ .

Recall the problem with the lepton tag. Only 20% of the  $B$ 's decay to an electron or muon; the acceptance for these is only about 40% (due to the  $P_t$  cut), and the vertexing efficiency is estimated at 33%. Hence only 2.7% of all decays could be tagged this way. [In the EOI, the 2 chances for an interesting  $B$  decay per  $B\bar{B}$  pair are included elsewhere in the bookkeeping.] Furthermore, all tagging will be subject to a  $p = 20\%$  mistagging probability due to mixing. The proper figure of merit is  $1 - 2p = 60\%$ , so the fraction of  $B$  decays effectively tagged by the lepton tag is only about 1.6%.

The Kaon tag would be based on the sign of the Kaon arising in the decay chain

$$b \rightarrow c \rightarrow s \rightarrow K^- \quad \text{or} \quad \bar{K}^0.$$

This chain occurs  $\sim 95\%$  of the time. [In Table 1 below, we suppose this chain occurs 100% of the time.] However, the  $b \rightarrow c$  transition includes the emission of a  $W^-$ , which can decay to a  $\bar{c}s$  combination about 33% of the time; then the  $\bar{c}$  decays to a  $\bar{s}$  essentially 100% of the time. The  $s(\bar{s})$  quark emerges as a  $K^-(K^+)$  50% of the time. The presence of a  $K^+$  could lead to a mistag. In the case of multiple Kaons, I suppose we just choose one at random to be the tagging Kaon, and suffer the consequences. Table 1 summarizes the probabilities of various qualities of tags occurring.

Table 1 ignores the small probability that an  $s\bar{s}$  pair is created from glue. This, and some of the 'Bad Tags' listed in the Table 1, could likely be suppressed by a momentum cut, not explored here. There is typically an extra Kaon in  $B_s$  decays, which would lead to bad tags. However,  $B_s$  decays are useless as tags because of their rapid oscillations; this dilution is already accounted for in the 20% mistagging probability due to mixing.

From Table 1 we see that  $45/72 = 62\%$  of all  $B$  decays could yield a Kaon tag, but that  $7/45 = 16\%$  of these would be a mistag. Actually, we must combine the mistags due to the wrong-sign Kaon with the mistags due to mixing. The total mistagging probability is  $(16\%)(80\%) + (84\%)(20\%) = 30\%$ . The tagging efficiency is then  $1 - 2p = 40\%$ . I estimate that the geometrical acceptance for the Kaon tag would be more like 70%, as we wouldn't need as strong a  $P_t$  cut as for the leptons. The vertexing efficiency is again about 33%. Hence the effective fraction of  $B$  events that could have a Kaon tag is  $(70\%)(33\%)(40\%) = 9\%$ .

Table 1. Estimates of the efficiency of a tag on the particle/antiparticle character of a  $B$  meson based on the sign of Kaons in the  $B$  decay.

$b \rightarrow c \rightarrow s \rightarrow$	$b \rightarrow W^- \rightarrow$	Good Tag Prob.	Bad Tag Prob.	No Tag Prob.
$K^-$	other	1/3		
$K^-$	$K^+ \bar{K}^0$	1/48	1/48	
$K^-$	$K^+ K^-$	2/72	1/72	
$K^-$	$K^0 \bar{K}^0$	1/24		
$K^-$	$K^0 K^-$	1/24		
$\bar{K}^0$	other			1/3
$\bar{K}^0$	$K^+ \bar{K}^0$		1/24	
$\bar{K}^0$	$K^+ K^-$	1/48	1/48	
$\bar{K}^0$	$K^0 \bar{K}^0$			1/24
$\bar{K}^0$	$K^0 K^-$	1/24		
Total		38/72	7/72	27/72

This is six times higher than the lepton tag. It is fairly likely that we could make this tag work for the  $B \rightarrow J/\psi X$  events, and so the tagged, reconstructed event sample in the EOI should be multiplied by up to 6. This would improve our sensitivity to  $\sin 2\varphi_1$  by 2.4, bringing it down to 0.05, as summarized in Table 2.

If a secondary-vertex trigger could be implemented, we might get this improvement in all tagged, reconstructed event samples.

These arguments reinforce the interest in exploring the trigger and tag in a mini-BCD experiment. Of course, we must have Kaon identification to implement the Kaon tag.

Table 2. Update of Table 11 of the EOI to include a Kaon tag for  $B_d^0 \rightarrow J/\psi K_S^0$ . The minimum values of  $\sin 2\varphi$  resolvable to three standard deviations in  $10^7$  sec of running at luminosity of  $10^{32} \text{ cm}^{-2}\text{sec}^{-1}$ . The dilution factor  $D$  due to mixing is given by  $x_q \coth(\pi/2x_q)/(1 + x_q^2)$ .

Angle	Mode	Tag	Tagged Events	$1 - 2p$	$b$	$x_q$	$D$	$\sin 2\varphi_{\min,3\sigma}$
$\varphi_1$	$B_d^0 \rightarrow J/\psi K_S^0$	$e^\pm$	14,400	0.60	0.1	0.7	0.47	0.094
$\varphi_1$	$B_d^0 \rightarrow J/\psi K_S^0$	$K^\pm$	110,000	0.40	0.1	0.7	0.47	0.053
$\varphi_2$	$B_d^0 \rightarrow \pi^+\pi^-$	$e^\pm$	60,000	0.60	1.0	0.7	0.47	0.062
$\varphi_3$	$B_s^0 \rightarrow \rho^0 K_S^0$	$e^\pm$	400	0.60	1.0	$\sim 10$	0.64	0.55
$\varphi_3$	$B_s^0 \rightarrow K^+K^-$	$e^\pm$	1,560	0.60	$\sim 0.1$	$\sim 10$	0.64	0.21